



# Soft Sequences in Real Analysis

Abdulsattar Abdullah hamad<sup>1\*</sup>, V. Amarendra Babu<sup>2</sup>

<sup>1</sup>Department of mathematics College of Science, Acharya Nagarjuna University, India

<sup>2</sup>Acharya Nagarjuna University, Nagarjuna Nagar-522510, India

\*Corresponding author E-mail: <sup>1</sup>satar198700@gmail.com

## Abstract

In This work is an attempt to present new class of limit soft sequence in the real analysis it is called ( limit inferior of soft sequence " and limit superior of soft sequence) respectively are introduced and given result an example with two new definitions and studied some of the properties of them are investigated.

**Keywords:** limit superior, limit inferior, soft sequences, Soft set, soft real numbers

## 1. Introduction

In an ongoing paper [35] S.Das, S.k. samanta, He exhibited two definitions which is soft real sets and soft real numbers along with properties and some documentation examples, Dubois and Prade [3] brought up that "Zadeh [11] utilized the word 'fuzzy' as alluding particularly to the presentation of shades or evaluations in entire/ bust ideas". As indicated by Zadeh [11], a fuzzy' set is a speculation, in the gullible sense, of a subset with limits "slow as opposed to unexpected or sharp". It is characterized by a participation work from a fundamental set to the unit interim and its cuts are sets. Diverse varieties of fuzzy sets are characterized by different researchers like Atanassov [2], Pawlak[10] etc., Anyway there is perplexity in the writing This is what is included between the word and its corresponding meaning in logic of fuzzy' Not accurate description' etc., which sort of allude to absence of adequate data, though the term 'fuzzy' expressly alludes to the possibility of steady change from 'yes' to 'no'. For example, by a fuzzy number [4], we generally mean a function  $f:R \rightarrow [0,1]$ , which is upper semi consistent, so that its  $\alpha$  -level set  $[f]_{\alpha}$  closed interval  $[a_{\alpha} b_{\alpha}]$ , for each  $\alpha \in (0,1)$  So it may be termed as 'fuzzy interval as commented by Dubios and Prade [3]

## 2. Preliminaries

### Definition 1.1 (Gradual element [3]).

A fuzzy (or graded) component 'e' in 'S' (where S is a given fresh set) is characterized by its task work a from  $L \setminus \{0\}$  to S, where S is finished with littlest component 0 and most prominent component 1. Thus given grade  $\lambda$   $a_e(\lambda) = S$  is the element of S which is the representation of e at level  $\lambda$ . The component (element) S itself has a task work  $a_e$  characterized just for  $\lambda = 1$  as  $a_s(\lambda) = S$

The idea of fuzzy element can be illustrated as follows:  
Consider a curved (convex) fuzzy set M of real line R .

Let  $m_{\alpha}$  be the center point of the  $\lambda - 1$  level of 'm'. then the set of pairs  $\{(\alpha, m_{\alpha}); \alpha \in (0,1]\}$  defines a fuzzy element of R.

### Definition 1.2 (Gradual set [3]):

A continuous (gradual) subset G in 'S' is characterized by its task work from  $L \setminus \{0\}$  to  $2^S$ , A solitary fuzzy component e yields a progressive singleton E by letting  $A_E(\lambda) = a_e(\lambda), \lambda \in L \setminus \{0\}$ . More for the most part, the continuous set G prompted by the group of fuzzy components  $e_1, e_2, \dots, e_k \in S$  with task F(x)  $a_1, a_2, \dots, a_k$  have its task (assignment) function  $a_G$  characterized by  $a_G(\lambda) = \{a_1(\lambda), a_2(\lambda), \dots, a_k(\lambda)\}, \forall \lambda \in \bigcup_{i=1}^k dom(a_i)$ .

### Definition 1.3 (Fuzzy set actuated by a progressive (gradual) set [3]):

The participation capacity of fuzzy set incited by the progressive set with task function  $a_G$  is  $\mu_G(s) = \sup\{\lambda; s \in a_G(\lambda)\}$  with a view to introduce only fuzziness in numbers, Dubios and Prade [3] introduce the following definition of gradual numbers by redefining fuzzy real numbers.

### Definition 1.4 (Gradual numbers [3]).

Definition 1.4 (Gradual numbers [3]). A continuous no of f can be demonstrated by a work  $A_f$  from the unit interim to the real line (and not the opposite).

Task on steady (Gradual) numbers [3]

Any operation between real numbers is extended to fuzzy real numbers  $r_1$  and  $r_2$  with assignment functions  $a_{\alpha}$  and  $a_{\beta}$  as  $a_{\alpha * \beta}(\lambda) = a_{\alpha}(\lambda) * a_{\beta}(\lambda) (a_{\alpha * \beta})(\lambda)$  is the assignment function of  $r_1 * r_2$ . It is to be noticed that the arrangement of every fuzzy number structures a gathering concerning expansion.

**Definition 1.5**

Soft set [9]. Let  $X$  be a non-empty crisp set and  $A$  be a set which is called index set. A pair  $(f, A)$  where  $f : A \rightarrow 2^X$  is a map, is said to be a soft set on  $X$ .

**Example of a Soft set 1.6 [9].**

Assume the accompanying:  $M$  is the arrangement of the houses Under thought and  $M = \{S_1, S_2, S_3, S_4, S_5, S_6\}$ .  $A$  is the set of parameter and  $A = \{e_1, e_2, e_3, e_4, e_5, e_6\} = \{\text{Beautiful, wooden, shoddy, in the green environment, in great repair}\}$ .

Assume that,

$F(e_1) = \{S_2, S_4\}, F(e_2) = \{S_1, S_3\}, F(e_3) = \{S_3, S_4, S_5\}, F(e_4) = \{S_1, S_3, S_5\}, F(e) = \{S_1\}$ , then the soft  $(F, A)$  can be looked as a gathering of approximations as underneath:

$(F, A) = \{\text{beautiful house} = \{S_2, S_4\}, \text{wooden house} = \{S_1, S_3\}, \text{shoddy houses} = \{S_3, S_4, S_5\}, \text{in the green surroundings houses} = \{S_1, S_3, S_5\} \text{ and in decent shape houses} = \{S_1\}\}$

**1.7 Soft Real Sets and Soft Real Numbers**

**Definition 1.8 [35]:**

(Soft element or component). Let  $Y$  be a non-vacant set and  $X$  be a non-vacant parameter set. At that point a function  $\varepsilon : X \rightarrow Y$  is said to be a soft component of  $Y$ . A soft component of  $Y$  is said to have a place with a soft set  $A$  of  $Y$ , meant by  $\varepsilon \in A$ , if  $\varepsilon(e) \in A(e), \forall e \in X$ . Thus a soft set  $A$  of  $Y$  concerning the index set  $X$  can be communicated as  $A(e) = \{\varepsilon(e), \varepsilon \in A\}, e \in X$

Note 1.9. [35]: It is to be noticed that each singleton soft set (a soft set  $(F, A)$  for which  $F(e)$  is a singleton set,  $\forall \lambda \in A$ ) can be related to a soft component by basically distinguishing the singleton set with the component that it contains  $\{\forall \lambda \in A\}$ .

**Definition 1.10. [35]:**

Let  $R$  be the set of real numbers,  $\wp(R)$  be the accumulation of all non vacant bounded subsets of  $R$  and  $A$  be a set of parameters. At that point a mapping  $F : A \rightarrow \wp(R)$  is known as a soft real set. It is meant by  $(F, A)$ , in particular is a singleton soft set, at that point relating  $(F, A)$ , to the comparing soft component, it will be known as a *soft real number*.

It can be easily checked that a fuzzy real number [4] is a special case of soft real set

when the parameter set is  $\{0,1\}$  and the  $\lambda$ -approximation sets are closed interval for every  $\lambda \in A$ . It can also be checked that the gradual (fuzzy) real numbers defined by Dubois and Prade [3] are soft real numbers with parameter set  $\{0,1\}$

**Example of soft real set.1.11.**

[35]: Here we give two different examples of soft real sets.

**Example 1.12. [35]**

Let  $R$  be the set of real numbers and  $A$  be a set of parameters given By  $A = \{e_1, e_2, e_3, e_4\}$ . By assume that

$$F(e_1) = \{3, 2, 1\}, F(e_2) = \{7, 5, 4, 3\}, F(e_3) = \{1, 3\}$$

$$F(e_4) = \{12, 41, 35, 6, 0\},$$

then the softreal set  $(F, A)$  can be looked as a gathering of approximations as underneath :

$$(F, A) = (e_1, \{1, 2, 3\}), (e_2, \{4, 5, 6, 7\}), (e_3, \{3, 7\}), (e_4, \{12, 41, 35, 6, 0\})$$

**Example 1.13.**

[35] Let  $R$  be the set of real numbers and  $A$  be a set of parameters given

$$\text{By } A = \{[1,10], [11,20], [21,30], [31,40], [41,50]\} = \{e_1, e_2, e_3, e_4, e_5\}$$

If  $F : A \rightarrow P(R)$  describes the numbers within the interval" then

$$F(e_1) = \{2, 3, 5, 7\}, F(e_2) = \{11, 13, 17, 19\}, F(e_3) = \{23, 29\}, F(e_4) = \{31, 37\}, F(e_5) = \{41, 43, 47\}$$

then  $(F, A)$  can be considered as a soft real set such that  $(F, A) = e_1\{2, 3, 5, 7\}, (e_2\{11, 13, 17, 19\})$

$$(e_3, \{23, 29\}), (e_4, \{31, 37\}), (e_5, \{41, 43, 47\})$$

**Example of soft real number 1.14.**

[35] We present two different examples of soft real Numbers.

**Example 1.15.**

[35] Suppose a Nursery school has six classes namely Nursery, KG, Class I, Class II, Class III and Class IV. There is various numbers of students in different classes. If we consider a parameter set  $A = \{\text{KG, Class I, Class II, Class III and Class IV}\}$  and define

$F : A \rightarrow P(R)$  by  $F(e) =$  the number of student in class  $e$ ,

if  $F(\text{Nursery}) = \{54\}$ ,  $F(\text{KG}) = \{51\}$ ,  $F(\text{class D}) = \{44\}$ ,  $F(\text{Class II}) = \{42\}$ ,  $F(\text{Class III}) = \{62\}$ ,  $F(\text{Class IV}) = \{49\}$  then identifying  $(F, A)$  with the corresponding soft element we get a soft real number  $(F, A)$  such tht  $(F, A) = \{\text{Nursery of student} = 54; \text{KG student} = 51; \text{Class I students} = 44, \text{Class II students} = 42, \text{Class III students} = 62, \text{Class IV students} = 49\}$

**Example 1.16.**

[35] Consider the example of soft set in If a mapping  $G : E \rightarrow P(R)$

be define by  $G(e)$  the number Of houses a available under the category  $e$ .

Then we have from 2.6,

$$G(e_1) = \{2\}, G(e_2) = \{2\}, G(e_3) = \{3\}, G(e_4) = \{3\}, G(e_5) = \{1\},$$

Then  $(G, E)$  identifying , with the corresponding soft element, it can be taken as a soft real

number such that  $G, E = \{\text{beautiful houses} = 2; \text{wooden houses} = 2; \text{cheap houses} = 3; \text{in the green surroundings houses} = 3; \text{in good repair houses} = 1\}$ . Let us denote the set of all soft real sets by  $R(A)$  and the set of all soft real numbers By  $\square(A)$ .

**3. Main Result**

Limit superior and limit inferior of soft sequences in Real analysis In this paper we will define limit superior and limit inferior of soft sequences. So will present some properties for them and for (finite, infinite) with two examples and given Result.

**Definition: 2.1.**

let  $\{\tilde{x}_n\}$  be a sequence (rename (seq) of soft Real numbers , and

$\lambda$  be a fixed real number the limit superior  $\limsup < \tilde{x}_n(\tilde{\lambda}) >$  of

soft seq  $\{\tilde{x}_n\}$

is defined by:

$$\limsup < \tilde{x}_n(\tilde{\lambda}) > = \inf_n \sup_{k \geq n} \tilde{x}_k(\tilde{\lambda}).$$

And,

The limit inferior  $\liminf < \tilde{x}_n(\tilde{\lambda}) >$  of soft seq  $\{\tilde{x}_n\}$

is defined by:

$$\liminf < \tilde{x}_n(\tilde{\lambda}) > = \sup_n \inf_{k \geq n} \tilde{x}_k(\tilde{\lambda}).$$

We have  $\lim \bar{< \tilde{x}_n(\tilde{\lambda}) >} = -\lim < \tilde{x}_n(\tilde{\lambda}) >$  and,

$$\lim [< \tilde{x}_n(\tilde{\lambda}) >] \leq \lim \bar{< \tilde{x}_n(\tilde{\lambda}) >}$$

Thus  $\text{seq} < \tilde{x}_n(\tilde{\lambda}) >$  is converges to an extended soft real numbers  $l$  if and only if

$$l = \lim < \tilde{x}_n(\tilde{\lambda}) > = \lim \bar{< \tilde{x}_n(\tilde{\lambda}) >}$$

**Definition:2.2 .**

let  $\{\tilde{x}_n\}$  be a seq of soft Real sets. Then the  $\text{seq}\{\tilde{x}_n\}$  is said to be soft converge to a soft real set 'X' if :

$$\limsup \bar{< \tilde{x}_n(\tilde{\lambda}) >} = \sup x(\tilde{\lambda})$$

and,  $\liminf \tilde{< \tilde{x}_n(\tilde{\lambda}) >} = \inf \tilde{x}(\tilde{\lambda}), \forall \lambda \in A$ .

$\{\tilde{x}_n\}$  is then said to be a soft convergent seq converging to the soft limit  $x$  and  $x_n \sim x$ .

**Example 2.3.**

let  $\{\tilde{x}_n\}$  be a seq of Real sets. Where

$$< \tilde{x}_n(\tilde{\lambda}) > = [\tilde{a}_\lambda + (1/\tilde{n})], < \tilde{x}_n(\tilde{\lambda}) > = [\tilde{b}_\lambda - (1/\tilde{n})],$$

$\forall \lambda \in A, n = 1, 2, 3$ .  $a_\lambda, b_\lambda$  are fixed real Numbers for each  $\lambda$ . Then for every  $\lambda \in A$ .

$$\lim < \tilde{x}_n(\tilde{\lambda}) > = \tilde{b}_\lambda \text{ and } \lim \bar{< \tilde{x}_n(\tilde{\lambda}) >} = \tilde{a}_\lambda.$$

Let  $a_\lambda = \zeta$  and,  $b_\lambda = \mu$  so  $x(\lambda) = (\zeta, \mu)$  and,

Let  $y(\lambda) = (\zeta_1, \mu_1)$ , then  $x, y \in R(A)$  and  $x \neq y$

but we know that by definition of soft convergence  $x_n \sim x$  and  $x_n \sim y$ .

**2.4 Properties of Limit Superior and Limit Inferior of Soft Sequences**

Let  $< \tilde{x}_n(\tilde{\lambda}) >, n \in N^+$  be a bounded seq then

$\alpha = \lim \bar{< \tilde{x}_n(\tilde{\lambda}) >} = \inf_n \sup_{k \geq n} < \tilde{x}_k(\tilde{\lambda}) >$  if and only if  $\in > 0$ ,

- 1- the  $\text{seq}\{n \in N^+ : < \tilde{x}_n(\tilde{\lambda}) > > \alpha + \in\}$  is finite
  - 2- the sequence  $\{n \in N^+ : < \tilde{x}_n(\tilde{\lambda}) > > \alpha - \in\}$  is infinite
- And,

$\beta = \lim < \tilde{x}_n(\tilde{\lambda}) > = \sup_n \inf_{k \geq n} < \tilde{x}_k(\tilde{\lambda}) >$  if and only if  $\in > 0$

- 1. The  $\text{seq}\{n \in N^+ : < \tilde{x}_n(\tilde{\lambda}) > > \beta + \in\}$  is finite
- 2. The  $\text{seq}\{n \in N^+ : < \tilde{x}_n(\tilde{\lambda}) > > \beta - \in\}$  is infinite.

**Result 2.5**

if  $< \tilde{x}_n(\tilde{\lambda}) >$  and  $< \tilde{y}_n(\tilde{\lambda}) >$  are two sequence then we have

$$\lim < \tilde{x}_n(\tilde{\lambda}) > + \lim < \tilde{y}_n(\tilde{\lambda}) > \leq$$

$$\lim < \tilde{x}_n + \tilde{y}_n >(\tilde{\lambda})$$

$$\leq \lim \bar{< \tilde{x}_n(\tilde{\lambda}) >} + \lim \bar{< \tilde{y}_n(\tilde{\lambda}) >}$$

$$\leq \lim \bar{< \tilde{x}_n + \tilde{y}_n >(\tilde{\lambda})}$$

$$\leq \lim \bar{< \tilde{x}_n(\tilde{\lambda}) >} + \lim \bar{< \tilde{y}_n(\tilde{\lambda}) >}$$

**Proposition 2.6:**

Let  $\{\tilde{x}_n\}$  be a soft convergent seq of negative or positive soft real sets converging to soft real set  $x$ , then  $\frac{1}{\tilde{x}_n}, \frac{1}{\tilde{x}}$  provided zero doesn't  $x(\tilde{\lambda})$  for any  $\lambda \in A$ .

**Proof:**

Since  $\tilde{x}_n \rightarrow x$ , and '0' is not a member of  $x(\lambda)$  for any  $\lambda \in A$ ,  $x$  is also either -ve or +ve soft real set. we have for every  $\lambda \in A$ ,

$$\lim \bar{< \tilde{x}_n(\tilde{\lambda}) >} = \inf_n \sup_{k \geq n} \tilde{x}_k(\tilde{\lambda}), \text{ and}$$

$$\lim < x_n(\lambda) > = \sup_n \inf_{k \geq n} \tilde{x}_k(\tilde{\lambda}), \lambda \in A,$$

We have for every  $\lambda \in A$  and  $n \in N$ ,

$$\sup \{1/(\tilde{x}_n(\tilde{\lambda}))\} = 1/\inf\{\tilde{x}_n(\tilde{\lambda})\} \text{ and}$$

$$\inf\{1/(\tilde{x}_n(\tilde{\lambda}))\} = 1/\sup\{\tilde{x}_n(\tilde{\lambda})\},$$

Taking limit superior and limit inferior,

$$\lim \bar{\sup}\{1/\tilde{x}_n(\tilde{\lambda})\} = \lim \inf\{1/\inf\{\tilde{x}_n(\tilde{\lambda})\}\}$$

$$1/\lim \inf\{\tilde{x}_n(\tilde{\lambda})\} = 1/\inf\{\tilde{x}(\tilde{\lambda})\}$$

$$= \sup\{1/\tilde{x}(\tilde{\lambda})\},$$

Also,

$$\lim \inf\{1/\tilde{x}_n(\tilde{\lambda})\} = \lim (1/\sup\{\tilde{x}_n(\tilde{\lambda})\})$$

$$= 1/(\lim \sup\{\tilde{x}_n(\tilde{\lambda})\})$$

$$= 1/\sup\{\tilde{x}(\tilde{\lambda})\} = \inf\{1/\tilde{x}(\tilde{\lambda})\}, \forall \lambda \in A$$

$$\therefore 1/x_n \square 1/x.$$

**Example:2.7**

suppose  $\text{seq}\{\tilde{x}_n\}$  of a soft real sets  $\ni \tilde{x}_n \square \tilde{x}$  then the soft  $\text{seq} 1/\tilde{x}_n$  need not converge to the soft real set  $1/\tilde{x}$ .

**Solution:**

Taking a  $\text{seq}\{\tilde{x}_n\}$  of a soft real Numbers we have

$< \tilde{x}_n(\tilde{\lambda}) > = \{-6, -4, -3, 1, 2, 3\}$  for every  $\lambda \in A$  for every  $n \in N$  And

$< \tilde{x}(\tilde{\lambda}) > = \{-6, 3\}$ , for every  $\lambda \in A$

$$\lim \bar{< \tilde{x}_n(\tilde{\lambda}) >} = \inf_n \sup_{k \geq n} \tilde{x}_k(\tilde{\lambda}) = \inf_n 3 = \sup \tilde{x}(\tilde{\lambda}),$$

$$\forall \lambda \in A,$$

$$\liminf < \tilde{x}_n(\tilde{\lambda}) > = \sup_n \inf_{k \geq n} \tilde{x}_k(\tilde{\lambda}) =$$

$$-6 = \inf \tilde{x}(\tilde{\lambda}), \forall \tilde{\lambda} \in A$$

so,  $x_n \square x$ , But  $\{1/(\tilde{x}_n(\tilde{\lambda}))\} = \{-1/6, -1/4, -1/3, 1, 1/2, 1/3\}$ , and

$$\{1/(\tilde{x}(\tilde{\lambda}))\} = \{-1/6, 1/3\}$$

$$\text{Now, } \liminf < 1/\tilde{x}_n(\tilde{\lambda}) > = \inf_n \sup_{k \geq n} 1/\tilde{x}_k(\tilde{\lambda}) = 1$$

$$\liminf < 1/\tilde{x}_n(\tilde{\lambda}) > = \sup_n \inf_{k \geq n} 1/\tilde{x}_k(\tilde{\lambda}) = 1/3$$

$\therefore 1/\tilde{x}_n$ , not soft converge, does not soft converge to the  $1/\tilde{x}$ .

## References

- [1] Hac Aktas and Naim Cagman, (2007), Soft sets and soft groups, *Informations Sciences*, 177, 2726-2735.
- [2] Atanassov K., Intuitionistic fuzzy sets, (1986), *Fuzzy Sets and Systems*, 20, 87-96.
- [3] Dubois D. and Prade H., (2008), Gradual elements in a fuzzy set, *Soft Comput*, 12, 165-175.
- [4] Fortin J., Dubois D. and Prade H., (2008), Gradual numbers and their applications to fuzzy interval analysis, *IEEE Transaction of Fuzzy Systems*, 16 (2), 388-402.
- [5] Klir G. J. and Yuan B., "Fuzzy sets and fuzzy logic, Theory and applications", Prentice-Hall of India Pvt.Ltd., (1997).
- [6] Maji P. K., Biswas R. and Roy A. R., (2003), On soft set theory, *Computers Math. Applic.*, 45, 555-562.
- [7] Maji P. K., Biswas R. and Roy A. R., (2001), Fuzzy soft sets, *The Journal of fuzzy Math.*, 9 (3), 589-602.
- [8] Majumdar P. and Samanta S. K., (2008), Similarity measure of soft sets, *World Scientific Publishing Compa Vol. 4, No.1*, 1-12.
- [9] Molodtsov D., (1999), Soft set theory-first results, *Computers Math. Applic*, 37 (4/5), 19-31.
- [10] Pawlak Z., Rough sets, (1982), *International Journal of Information and Computer Sciences*, 11, 341-356.
- [11] Zadeh L.A., Fuzzy sets, (1965), *Infor. And Control*, 8, 338-353.
- [12] Karadogan A, (2008) Application of fuzzy set theory in the selection of underground mining method, *Journal of the southern African institute of mining and metallurgy*, vol. 108, pp. 73-79
- [13] Atagun A.O. and Sezgin A, (2011), Soft substructures of rings, fields and modules, *Computers and Mathematics with applications* 61, 592-601.
- [14] Sezgin A. and Atagun A. O., (2011), On Operation of soft sets, *Computers and Mathematics with applications* 61, 1457- 1467
- [15] Kharal A. and Ahmad B, (2010), Mappings on soft classes, *Inf. Sci.*, INS-D-08-1231 by ESS, pp. 1-11
- [16] Chen D., Tsang E. C. C., Yeung D. S. and Wang X, (2005), The parameterization reduction of soft sets and its application, *Comp. Math. with appl.* 45, 757-763.
- [17] Sut D.K., (2012), An Application of Fuzzy Soft Relation in Decision Making Problems, *Int. Journal of Mathematics Trends and Technology*, Vol.3 Issue 2. 201-205
- [18] Feng F., Jun Y. B. and Zhao X., (2008), Soft semi rings, *Computers Math. Applic.* 56, 2621-262.
- [19] Prade H. and Dubois D., "Fuzzy Sets and Systems: Theory and Applications", Academic Press, London, 1980.
- [20] Zimmerman H.J., "Fuzzy Set Theory and Its Applications", Kluwer Academic, Boston, MA, 1996.
- [21] ktas H.A and Cagman N., (2007), Soft sets and Soft groups, *Information Sciences* 177, 2726-2735
- [22] Yang H. and Guo Z., (2011), Kernels and closures of soft set relations, and soft set relation mappings, *Comp. Math. Appl.* 651-662
- [23] Ghosh J., Dinda B. and Samanta T. K, (2011), Fuzzy Soft Rings and Fuzzy Soft Ideals, *Int. J. Pure Appl. SCI. Technol.*, 2(2), pp. 66-74.
- [24] Zhou J., Li Y. and Yin Y, (2011), Intuitionistic fuzzy soft set semigroups, *Mathematics Aeterna*, vol. 1, No. 03, 173-183.
- [25] Atanassov K., (1994), Operators over interval valued intuitionistic fuzzy sets, *fuzzy sets and systems*, 64, 159-174
- [26] Babitha K.V. and Sunil J.J. (2011), Soft sets relations and functions, *Computers Math. Applic* 60, 1840- 1849.
- [27] Gong K., Xiao Z. and Zhang X. (2010), The bijective soft set with its operations, *Computers and Math. Appl.* 60, 2270- 2278.
- [28] Qin K. and Hon Z., (2010), On soft equality. *Computers Math. Appl.* 234, 1347-1355.
- [29] Irfan Ali M., Feng F., Liu X., Min W. K. and Shabir M, (2009), On some new operations in soft set theory, *Comp. and Math. With appl.* 57, 1547- 1553
- [30] Ozturk M.A. and Inan E., (2011), Soft  $\Gamma$  - rings and idealistic soft  $\Gamma$  - rings, *annals of fuzzy Mathematics and informatics volume 1*, no. 1, pp. 71-80.
- [31] Mushrif M.M., Sengupta S, and Ray A. K., (2006), Texture Classification Using A Novel, Soft Set Theory Based Classification Algorithm, *LNCS 3851*, pp. 246-254 2006
- [32] Cagman N., Citak F., and Enginoglu S., (2011), FP-soft set theory and its applications, *annals of fuzzy math.inform.vol. 2,no.2*, pp.219-226
- [33] Cagman N., Citakand F., Enginoglu S, (2010), fuzzy parameterized fuzzy soft set theory and its applications, *journal of Turkish fuzzy systems association. vol.1.no.1*, pp.21-35.
- [34] Hassan R.N., Tantawy O.A, (2016), Soft Real Analysis, *journal of progressive Research in Mathematics*, vol 8, issue 1, 65-69
- [35] Das S., samanta S.k., (2012), soft real sets, soft real numbers and their properties, *Journal of fuzzy mathematics* vol.20.No.3, 551
- [36] Maji P.K., ROY AR. and Biswas. R, (2002), An application of soft set in a decision making problem computers and mathematics with application 44(8/9), 1077-1083.
- [37] Mane maran (2011), on fuzzy soft groups *Int, journal of comp.Applications*, vol.15,no7, 38
- [38] Alkhazaleh.A.salleh and hassan N., (2011), Soft multiset theory, *Applied mathematical sciences*, vol.5,No72 ,3561-3573.2011.
- [39] Herawan T., Ghazali R. and Deris M.M.D (2010), Soft set theoretic approach for dimensionality reduction, *Information journal of Database theory and Application* vol.3, No.2, 47-60
- [40] Xu W. (2010), Vague soft sets and their properties, *Computers and mathematics with applications* 59, 787-794,.
- [41] Ge X. and yan S., (2011), Investigation on some operation of soft sets. *word academy of science, eng. And tech.* 75, 1113 – 1116.
- [42] Jun Y.B., Kimand H.S, Park C.H (2011), Positive implicative ideals of BCK-algebras based on soft set theory, *Bull.malays .math.sci-soc.* 34 (2), 345-354
- [43] Jun Y.B., Lee K.J. and Park C.H., (2008), Soft set theory applied to commutative ideals in BCK-Algebras *J.Appl.math.and informatics*, vol.26, no.3-4, pp 707-720.
- [44] Pawlak Z., Hard And soft sets, *proceeding of the international Eorkshop on Rough sets and knowledge Discovery, Banff, 1993*