

Development of Algorithm for Dynamic Hybrid Mean/Median Filter using Adaptive Window Selection Approach to Eliminate Salt & Pepper Noise

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Abstract

The research work aimed to develop a new Dynamic Hybrid Mean/Median Filter (DHMMF) algorithm to eliminate salt & pepper noise. The proposed DHMMF algorithm decides window size dynamically during runtime, also adaptively adjusts window size based on the non-noisy pixels present in a local window. Window size is limited to 9 X 9. This reduces blurring and computational complexity. Filter is designed with two stages, noise detection succeeded by filtering strategy. During the noise detection stage, if pixel intensity value is in-between 1 to 254, it is classified as a non-noisy pixel and left unchanged. Pixel having 0 or 255 intensity value is classified as a noisy pixel. During the filtering stage, a noisy pixel is replaced with mean, median or trimmed values within a local window depending on various algorithmic conditions. Performance of DHMMF algorithm is compared with various existing methods. Performance is tested for low, medium and high density noise. Simulation results demonstrate that image quality is retained by preserving fine details and edges which results in better visual quality. Quantitative and qualitative analysis is carried out using PSNR and SSIM respectively.

Keywords: Adaptive; Filter; Multimedia Data; Noisy Data; Salt Pepper Noise.

1. Introduction

Salt & Pepper noise gets introduced in images during the acquisition process, faulty memory location, atmosphere conditions, bit error during transmission, synchronization error and malfunction in capturing devices like misaligned lenses, camera sensors and weak focal length [1], [2]. Such noisy image pixels exhibit either minimum 0 or maximum 255 gray level intensity value. This causes the image quality degradation and loss of fine edges [3], [4].

In multimedia data, de-noising is a necessary pre-processing step for image processing operations. It is required to eliminate the noise to restore the data. There are various linear and non-linear filtering methods exists [5 - 12]. For additive noise, linear filtering is useful, but it blurs the image and losses fine details. Hence most methods use non-linear filter to preserve fine details and edges. Median filter is simple robust which replaces all pixels with median of neighborhood pixels present in a current local window. This achieves acceptable results in low noise densities but results in a blur image and it also process non-noisy pixels. The proposed DHMMF algorithm developed to retain a high-quality image and it is compared with various existing methods.

In this research paper, Section 2 explains the noise model, Section 3 describes a new DHMMF algorithm, Section 4 gives various adaptive window scenarios, Section 5 explains performance measures, Section 6 demonstrate comparison and simulation results, Section 7 the conclusion of research objective.

2. Noise Model

Salt & Pepper noise consists of pixels with minimum value $r_{min} = 0$ and maximum value $r_{max} = 255$. Progressively white pixel values will be present in the dark region and vice versa. A noisy image with Salt & pepper noise [2] defined as:

$$Z(i,j) = \begin{cases} r_{min} & \text{with probability } p_1 \\ p(i,j) & \text{with probability } 1 - p_1 - p_2 \\ r_{max} & \text{with probability } p_2 \end{cases} \quad (1)$$

where

$Z(i,j)$ is a noisy image

$p(i,j)$ is a non-noisy pixel.

197	123	110
180	156	77
56	109	94

→

197	123	110
180	0	77
56	109	94

Fig. 1: Image Metrics 3 X 3 with a Corrupted Central Pixel.

Consider 3 X 3 image metrics as shown in Figure 1. Suppose salt & pepper noise is introduced in the image, a central pixel value i.e. 156, is changed to 0.

3. Proposed DHMMF Algorithm

The proposed DHMMF algorithm combines the advantages of both mean and median filter. Current local window size is considered as threshold value. If the number of non-noisy pixels <

threshold, then window size is increased by $W=W+2$ till it reaches the maximum window size limit $W=9$ to avoid blurring and computational complexity. A noisy pixel is detected and replaced with below algorithmic conditions.

Input : The noisy image Z
Output : The filtered image X

- Step 1 : Set $W = 3, h = 2, W_{max} = 9$
- Step 2 : Processing starts with a sub-window $W \times W$. Consider the center pixel as Z_{ij}
- Step 3 : If $0 < Z_{ij} < 255$, then keep Z_{ij} unchanged. Shift to next sub-window.
Go to Step 1
- Step 4 : If the center pixel $Z_{ij} = 0$ or $Z_{ij} = 255$ then it is considered as corrupted pixels.
- Step 5 : Pixels except 0 and 255 are collected in S
- Step 6 : If $size(S) \geq W_{current}$ and $W_{current} \leq W_{max}$ then replace Z_{ij} with **Median**(S)
Go to Step 10
- Step 7 : If $size(S) < W_{current}$ and $W_{current} \leq W_{max}$ then window size is increased as $W = W_{current} + h$
Go to Step 2
- Step 8 : If $size(S) < W_{current}$ and $W_{current} = W_{max}$ then replace the center pixel Z_{ij} as per following cases:
 Case 1 : If $size(S) < 7$ then replace Z_{ij} with **Mean**(S)
Go to Step 10
 Case 2 : If $size(S) \geq 7$ then replace Z_{ij} with **Median**(S)
Go to Step 10
- Step 9 : If $W_{current} \geq W_{max}$ then replace the center pixel Z_{ij} as per following cases:
 Let $A = \{0\}$ and $B = \{255\}$
 Case 1 : If $v \in A$ then replace Z_{ij} with 255
Go to Step 10
 Case 2 : If $v \in B$ then replace Z_{ij} with 0
Go to Step 10
 Case 3 : If $v \in (A \cup B)$ then replace Z_{ij} with **Mean**(v)
Go to Step 10
- Step 10 : Select next sub-window $W \times W$. Repeat Step 2 to Step 7

Summary of DHMMF Filter algorithm implementation approach:

- Proposed algorithm is applied on a noise image, $Z(i, j)$

$$g(i, j) = EDHMMF(Z(i, j)) \tag{2}$$

- Filtered image is restored as,

$$h(i, j) = \begin{cases} Z(i, j) & (i, j) \text{ uncorrupted pixels} \\ g(i, j) & \text{other pixels} \end{cases} \tag{3}$$

4. Adaptive Window Scenarios

- Center pixel intensity value is except 0 and 255. It will considered as a non-noisy pixel and keep it unchanged.

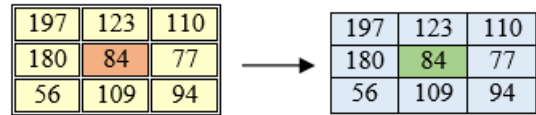


Fig. 2: Scenario 1.

- Center pixel intensity value is 0, indicates noisy pixel. Current window size is $W = 3$.
 $S = \{197, 123, 110, 180, 77, 56, 109, 94\}$, $size(S) = 8$
 As $size(S) > W$, the center pixel is replaced with **median**(S).

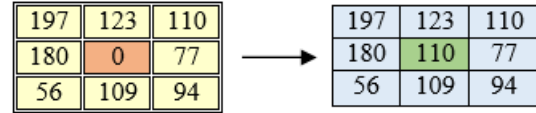


Fig. 3: Scenario 2.

- Center pixel intensity value is 0, indicates noisy pixel. Current window size is $W = 3$.
 $S = \{197, 123\}$, $size(S) = 2$
 Here $size(S) < W$, W is increased to $W+2$.
 $S = \{67, 99, 102, 197, 123, 100, 10, 6, 12, 120, 111\}$
 As $size(S) > W$, the center pixel is replaced with **median**(S).

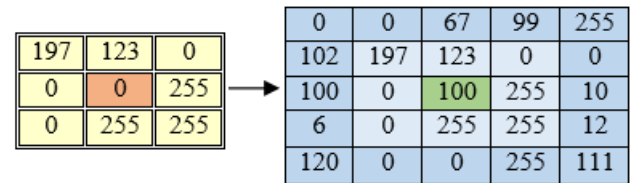


Fig. 4: Scenario 3.

- Center pixel intensity value is 0, indicates noisy pixel. Current window size W is expanded till $W=9$ until $size(S) > W$. Suppose maximum window size is reached.
 $S = \{98, 52, 8, 4, 155, 6\}$, $size(S) = 6$
 As $size(S) < 7$, the center pixel is replaced with **Mean**(S)

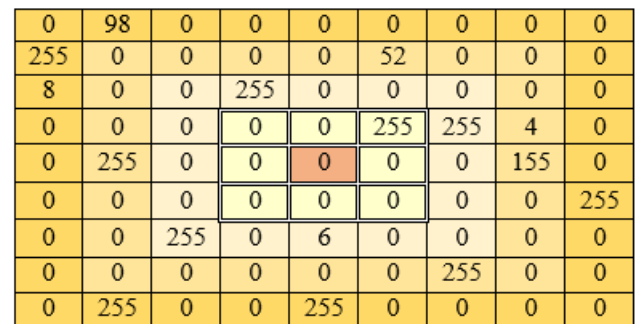


Fig. 5: Scenario 4.

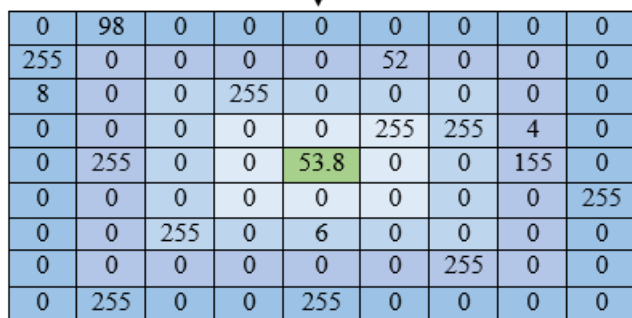


Fig. 5: Scenario 4.

- Center pixel intensity value is 0, indicates noisy pixel. Current window size W is expanded till $W=9$ until $size(S) > W$. Suppose maximum window size limit is reached.
 $S = \{8, 98, 89, 44, 100, 66, 6, 52, 102\}$, $size(S) = 9$

As size(S) > 7, the center pixel is replaced with *Median(S)*

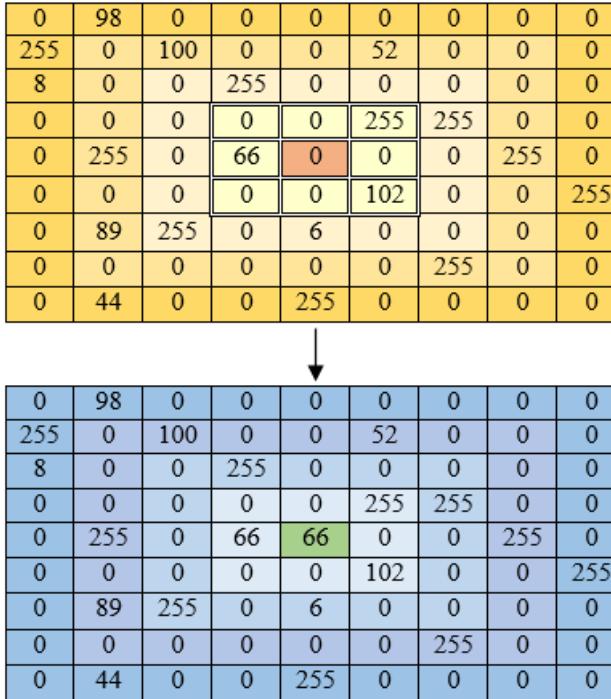


Fig. 6: Scenario 5.

- 6) Center pixel intensity value is 0, indicates a noisy pixel. Current window size W is expanded till W=9 until size (S) > W. Suppose maximum window size limit is reached and all pixels are with intensity value 0, then replace the center pixel with intensity value 255.

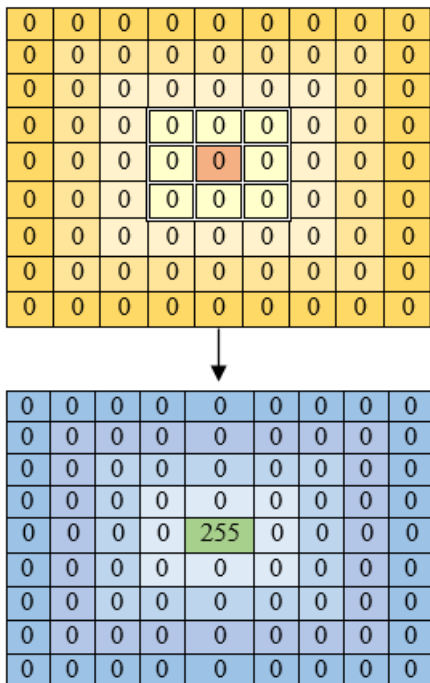


Fig. 7: Scenario 6.

- 7) Center pixel intensity value is 255, indicates noisy pixel. Current window size W is expanded till W=9 until size (S) > W. Suppose maximum window size limit is reached and all pixels are with intensity value 255, then replace the center pixel with intensity value 0.

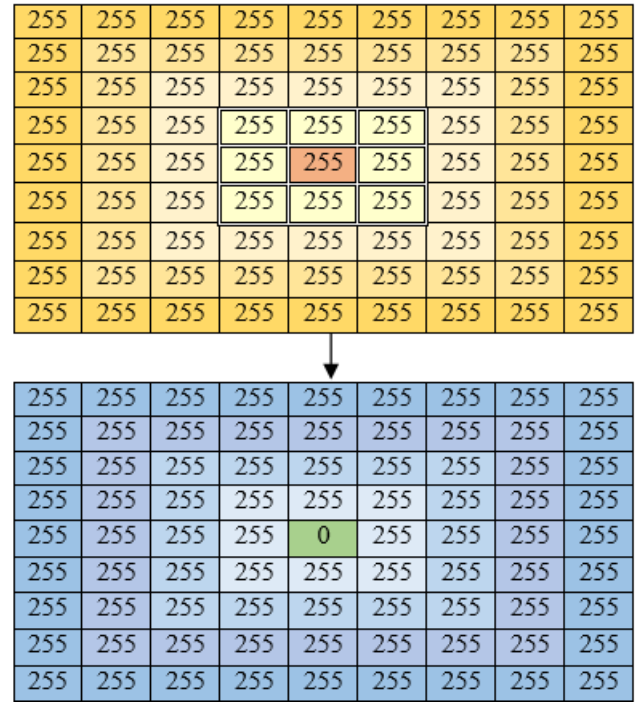


Fig. 8: Scenario 7.

- 8) Center pixel intensity value is 255, indicates a noisy pixel. A current window size W is expanded till W=9 until size (S) > W. Suppose maximum window size limit is reached and all pixels having intensity value 0 or 255, then replace the center pixel with *Mean(v)*.

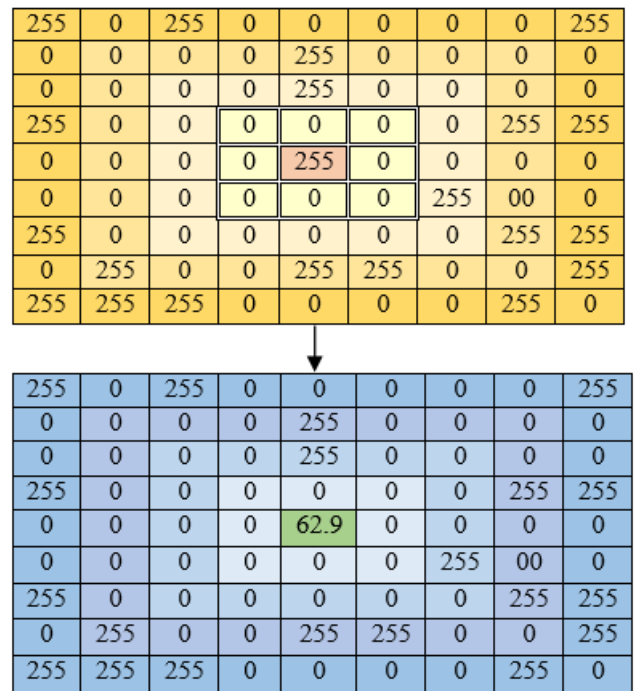


Fig. 9: Scenario 8.

5. Performance Measures

- 1) PSNR: Watermarked image quality is estimated with respect to an original image using PSNR.

$$PSNR = 10 \log_{10} \frac{Z_{max}^2}{\frac{1}{MN} \sum_{i,j} [q(i,j) - p(i,j)]^2}$$

where $Z_{max} = 255$

$p(i, j)$ is intensity values of an input image
 $q(i, j)$ is intensity values of the watermarked image

- 2) SSIM: Structured similarity is measured by considering luminance, correlation and contrast.

$$SSIM = \frac{(2\mu_f \mu_h + C_1)(2\sigma_{fh} + C_2)}{(\mu_f^2 + \mu_h^2 + C_1)(\sigma_f^2 + \sigma_h^2 + C_2)} \quad (5)$$

where $C_1 = (P_1 * G)^2$, $C_2 = (P_2 * G)^2$
 $G = 255, P_1 = 0.01, P_2 = 0.03$
 μ_f and μ_h are average of f and h respectively
 σ_f and σ_h are variance of f and h respectively

6. Experimental Results

Performance of DHMMF algorithm is tested for low, medium and high noise density. Fifteen different 512 X 512 size images are taken for the experiment. Simulations are performed using MATLAB 2018b for noise density ranging from 10% - 90% shown in Figure 10. SSIM index map is shown in Figure 11. DHMMF algorithm compared with various algorithms. Qualitative results in terms of PSNR values and quantitative results in terms of SSIM are shown in Table 1 and Table 2. Figure 12 and Figure 13 demonstrate that DHMMF algorithm gives better performance with high PSNR and SSIM by retaining image quality.



Fig. 10: The Simulation Result of Noisy Images ('a', 'b', 'c', 'd', 'e', 'k', 'l', 'n', 'o') and Respective Filtered Images ('f', 'g', 'h', 'i', 'j', 'p', 'q', 'r', 's', 't').

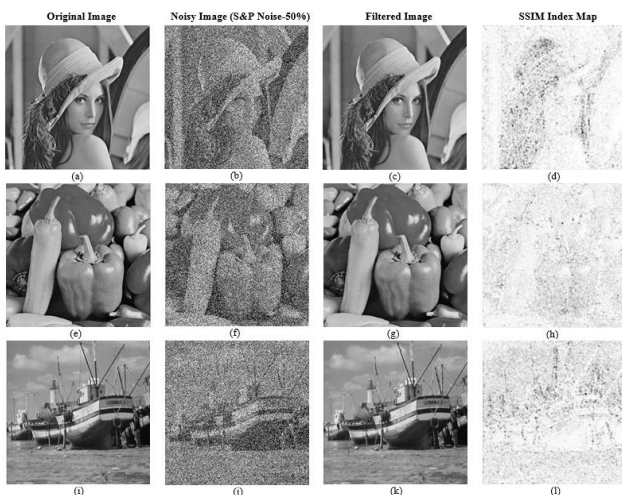


Fig. 11: Original Images - ('a', 'e', 'i'), Noisy Images - ('b', 'f', 'j'), Filtered Images - ('c', 'g', 'k'), SSIM Index Map - ('d', 'h', 'l').

Table 1: Comparison of PSNR And SSIM Values of Various Methods for Fifteen Test Images with 50% Noise Density

Test Images	Proposed DHMMF Algorithm		BPDF [5]		MDBU TMF [6]		EMF1[7]		EMF2[7]		NAFS M [8]	
	P	S	P	S	P	S	P	S	P	S	P	S
	SNR	SI	SNR	SI	SNR	SI	SNR	SI	SNR	SI	SNR	SI
Lena	32.7	0.9	29.8	0.8	23.6	0.5	26.7	0.8	29.7	0.8	31.5	0.9
	36.3	0.9	31.2	0.8	28.4	0.6	28.7	0.8	30.9	0.8	32.0	0.9
	35.5	0.9	30.3	0.8	27.7	0.5	27.6	0.8	30.5	0.8	31.2	0.9
	33.3	0.9	28.5	0.8	25.7	0.5	25.6	0.8	28.5	0.8	29.2	0.9
	31.9	0.9	27.8	0.8	25.0	0.5	25.0	0.8	27.8	0.8	28.6	0.9
Pepper	55.7	0.9	76.6	0.9	71.5	0.8	88.0	0.9	10.2	0.2	56.8	0.9
	4.9	0.9	0.3	0.3	1.4	0.4	0.0	0.0	4.7	0.7	3.1	0.1
	29.4	0.8	26.6	0.8	28.7	0.8	25.7	0.7	27.8	0.8	27.8	0.8
	99.7	0.9	41.6	0.4	69.1	0.5	99.3	0.9	53.6	0.5	73.9	0.9
	0.9	0.5	5.3	0.3	5.6	0.6	8.7	0.8	6.3	0.3	9.2	0.5
House	32.1	0.9	28.2	0.8	30.3	0.8	25.1	0.8	28.7	0.8	30.8	0.9
	29.3	0.9	25.5	0.8	27.5	0.9	25.8	0.8	25.9	0.9	25.1	0.8
	4.5	0.9	5.5	0.6	5.9	0.5	4.4	0.6	4.0	0.5	5.1	0.8
	30.9	0.8	28.4	0.8	28.0	0.8	25.4	0.8	27.0	0.8	28.0	0.8
	30.2	0.8	26.4	0.8	28.8	0.8	25.8	0.8	27.5	0.8	28.7	0.8
Cameran	26.7	0.8	24.4	0.8	24.1	0.8	23.9	0.8	24.8	0.8	25.4	0.8
	0.1	0.8	0.2	0.8	0.4	0.9	0.5	0.8	0.0	0.8	0.4	0.9
	26.1	0.8	24.2	0.8	24.1	0.8	23.5	0.8	24.0	0.8	25.1	0.8
	7.9	0.8	9.2	0.8	3.1	0.9	5.2	0.8	0.0	0.8	4.1	0.9
	30.4	0.8	28.1	0.8	28.0	0.8	25.4	0.8	27.0	0.8	28.7	0.8
Barbara	26.6	0.8	24.3	0.8	24.9	0.8	23.2	0.8	24.7	0.8	25.8	0.8
	0.1	0.8	0.2	0.8	0.4	0.9	0.5	0.8	0.0	0.8	0.4	0.9
	26.1	0.8	24.2	0.8	24.1	0.8	23.5	0.8	24.0	0.8	25.1	0.8
	7.9	0.8	9.2	0.8	3.1	0.9	5.2	0.8	0.0	0.8	4.1	0.9
	30.4	0.8	28.1	0.8	28.0	0.8	25.4	0.8	27.0	0.8	28.7	0.8
Baboon	23.7	0.8	22.3	0.7	23.4	0.7	22.0	0.7	23.4	0.7	23.1	0.7
	59.7	0.8	74.3	0.9	03.5	0.5	48.1	0.7	30.5	0.6	69.3	0.8
	8.9	0.7	1.3	0.4	0.2	0.3	1.1	0.6	1.7	0.7	0.0	0.7
	30.9	0.8	28.6	0.8	29.8	0.8	25.6	0.8	28.1	0.8	29.1	0.8
	45.0	0.8	94.6	0.6	02.8	0.1	51.6	0.0	20.1	0.1	29.6	0.2
Golghil	31.1	0.8	27.7	0.8	29.7	0.8	25.5	0.7	29.3	0.8	29.7	0.8
	13.2	0.8	18.3	0.7	45.4	0.9	31.9	0.0	67.5	0.7	86.4	0.6
	8.0	0.1	1.7	0.3	2.9	0.2	0.0	0.0	0.7	0.8	1.6	0.7
	31.9	0.8	29.0	0.8	29.5	0.8	25.7	0.8	28.3	0.8	28.7	0.8
	63.6	0.8	29.3	0.8	34.5	0.7	98.1	0.5	48.6	0.2	46.7	0.7
Coin	30.9	0.8	26.9	0.8	29.1	0.8	25.9	0.8	27.7	0.8	30.2	0.9
	86.4	0.8	45.9	0.9	15.9	0.8	57.4	0.4	12.1	0.5	16.2	0.6
	7.9	0.3	3.7	0.6	5.5	0.3	5.3	0.6	5.4	0.6	5.6	0.3
	30.9	0.8	26.9	0.8	29.1	0.8	25.9	0.8	27.7	0.8	30.2	0.9
	24.1	0.8	22.7	0.8	23.3	0.8	21.6	0.8	22.5	0.8	22.8	0.8
Forest	14.8	0.8	48.4	0.8	38.8	0.8	43.8	0.8	06.8	0.8	10.8	0.8
	0.4	0.1	2.2	0.2	3.1	0.3	4.1	0.4	2.5	0.6	6.4	0.4

		7	5	2	8	3	7				
				7	0	5	7				
Pea rs	36	0.	32	0.	34	0.	27	0.	34	0.	35
	.6	9	.8	8	.3	8	.6	8	.1	9	.6
	87	3	57	8	46	9	73	3	96	0	15
	8	1	7	6	8	6	9	8	7	6	3
				9	6	3	6				
On- ion	33	0.	27	0.	31	0.	26	0.	29	0.	31
	.3	9	.7	8	.9	9	.0	8	.0	9	.7
	12	5	58	6	13	1	10	3	58	0	20
	0	0	7	8	8	2	9	5	5	7	2
				4	7	8					
Tap e	32	0.	29	0.	29	0.	27	0.	31	0.	31
	.6	9	.2	8	.9	8	.2	8	.7	9	.9
	58	1	25	7	99	5	03	5	85	1	71
	3	8	6	6	3	5	0	4	4	7	2
				7	9	0					

Table 2: Comparison of PSNR and SSIM Values of Various Methods for 'Leena' Image with Noise Density 10-90%

Noise density (%)	Proposed DHMMF Algorithm		BPDF [5]		MDBUTMF [6]		EMF1[7]		EMF2[7]		NAFSM [8]	
	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM
10	42	0.9	39	0.9	39	0.9	39	0.9	40	0.9	38	0.9
	.4	9	.4	8	.0	8	.8	8	.3	8	.4	8
	88	1	90	3	72	0	84	6	58	7	41	3
	9	2	7	8	0	8	3	7	8	5	2	0
20	38	0.9	36	0.9	35	0.9	36	0.9	37	0.9	35	0.9
	.8	8	.1	6	.8	6	.5	7	.0	7	.8	6
	02	0	61	7	43	0	51	2	72	4	66	7
	6	6	8	8	0	1	1	3	6	7	6	6
30	36	0.9	33	0.9	32	0.9	32	0.9	34	0.9	34	0.9
	.1	6	.7	4	.7	1	.9	4	.3	5	.0	5
	35	7	97	7	49	9	75	8	96	5	62	1
	9	0	7	6	8	2	4	2	1	5	4	9
40	34	0.9	31	0.9	28	0.9	29	0.9	32	0.9	32	0.9
	.2	5	.3	2	.5	0	.8	1	.0	3	.6	3
	92	1	38	0	73	2	99	0	47	0	33	3
	0	6	7	0	7	0	7	0	5	7	8	9
50	32	0.9	29	0.9	23	0.9	26	0.9	29	0.9	31	0.9
	.7	3	.2	8	.6	7	.7	4	.7	9	.5	0
	36	3	61	3	41	1	88	3	45	7	5	4
	5	3	5	5	7	7	7	6	5	5	2	2
60	31	0.9	26	0.9	19	0.9	23	0.9	27	0.9	29	0.9
	.1	9	.4	8	.6	3	.1	7	.0	8	.3	8
	73	1	85	2	13	3	15	2	40	4	62	6
	0	1	5	6	8	6	7	6	2	4	2	5
70	29	0.9	23	0.9	16	0.9	19	0.9	24	0.9	27	0.9
	.4	8	.5	7	.4	1	.2	5	.7	7	.0	8
	46	7	11	3	07	7	37	7	88	2	57	0
	5	5	2	9	7	9	5	0	9	9	5	5
80	27	0.9	18	0.9	14	0.9	15	0.9	21	0.9	24	0.9
	.7	8	.3	5	.0	0	.2	3	.4	6	.6	7
	57	3	11	6	99	9	98	9	98	4	40	9
	2	4	1	2	7	8	9	6	7	9	1	1
90	25	0.9	11	0.9	12	0.9	11	0.9	16	0.9	21	0.9
	.2	7	.0	2	.7	0	.0	1	.8	4	.6	6
	09	1	14	8	48	9	05	7	29	3	19	8
	9	0	0	0	1	3	9	4	7	2	2	2

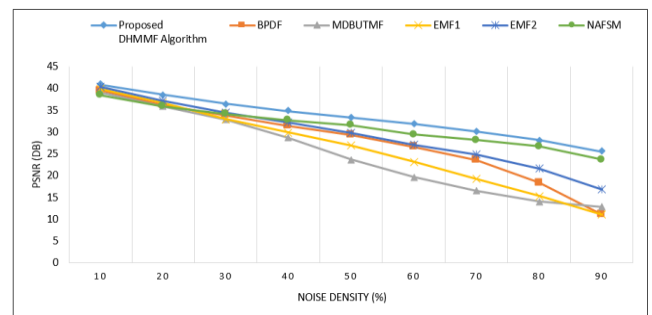


Fig. 12: Comparison of PSNR Values for Various Algorithms.

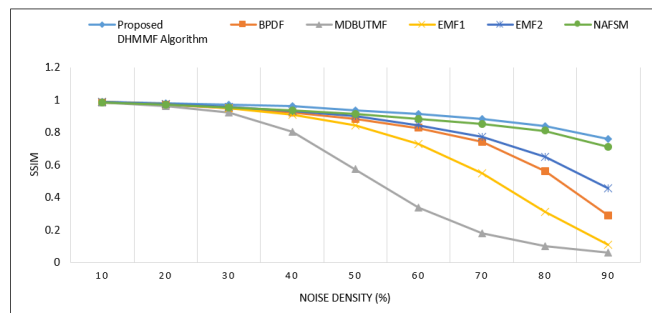


Fig. 13: Comparison of SSIM Values for Various Algorithms.

7. Conclusion

This paper concludes basic concepts and development of a new Dynamic Hybrid Mean/Median Filter (DHMMF) algorithm to eliminate salt & pepper noise. Filter is designed with two stages, noise detection succeeded by filtering strategy. DHMMF algorithm process only the noisy pixels. Filter decides window size dynamically during run time and also adaptively adjusts the window size based on non-noisy within a local window. Window size starts with 3 X 3 and expands up to 9 X 9. Window size is limited to 9 X 9 which results in a reduction of blurring and computational complexity. Threshold value chosen is the size of a current local window. Based on various algorithmic conditions DHMMF algorithm is tested for low, medium and high noise densities. Simulation results shows that image quality is retained by preserving details of an image. Quantitative and qualitative analysis shows higher PSNR and SSIM values, also results in better visual quality

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