

# Effects of Coil Pitch Spacing on Heat Transfer Performance of Nanofluid Turbulent Flow through Helical Microtube Heat Exchanger

A.H. Rasheed<sup>1\*</sup>, H. Alias<sup>1</sup>, S.D. Salman<sup>2</sup>

<sup>1</sup>Chemical Engineering Department, Faculty of Chemical and Energy Engineering, Universiti Teknologi Malaysia, Johor, Malaysia

<sup>2</sup>Al- Khwarizmi College of Engineering, University of Baghdad, Baghdad, Iraq

\*Corresponding author E-mail: [adnan\\_akeedy@yahoo.com](mailto:adnan_akeedy@yahoo.com)

## Abstract

This article provides Numerical simulation on forced convective heat transfer performance of Nanofluid flowing through copper helical microtube of inner diameter of 1.5 mm with different pitch using ANSYS-FLUENT 18.0. The simulation was performed for water, CuO/water, Al<sub>2</sub>O<sub>3</sub>/water Nanofluid with 1-2% volume concentration and different pitch of microtube (10, 14 and 18 mm) for turbulent flow regime of Reynolds number varied 5000 to 20000 and governing equations of mass, momentum and heat transfer were solved simultaneously, using the k-ε two equations turbulence model. Based on the obtained results, regardless of the concentrations used, the nanofluids exhibited a higher transfer rate than water. This is mainly attributed to the nanoparticles that are in the used nanofluids. The friction factor and the heat transfer rate were enhanced considerably due to the shape and size of the tube, which in this case is a helical microtube. Moreover, the maximum heat transfer performance has been conducted by Al<sub>2</sub>O<sub>3</sub>/water Nanofluid with 2% volume concentration and microtube pitch of 18 mm.

**Keywords:** Heat transfer enhancements, Helical micro coil Nanofluids, Mathematical model

## 1. Introduction

Heat Transfer Enhancement or Intensification is a technique in heat a transfer system which refers to thermal performance improvement. The effect of the improvements that is caused by the use of these techniques, leads to heat transfer systems to be smaller in size, and cheaper when it comes to the cost. These systems are widely used in many industries such as transportations, air-conditioning systems, cooling systems, nuclear reactors, cooling of electronic parts, space and defense, optical and biomedical applications. [1].

In general, the enhancement techniques classified into two categories. The nature of this categorization is based on whether or not these techniques have a dependency or need on external power. Techniques that are dependent on the external source are known as active techniques, while those that do not have such dependency are known as passive techniques. Examples of active techniques can be described as electric fields, jet impingement, acoustic or surface vibration, while passive type technique examples are types of surfaces, (rough, extended and treated), fluid additives (Nanofluids) and special surface geometries to the flow channel by incorporating inserts. Two or more passive and/or active techniques in the context of the compound technique may be used to produce an enhancement higher than each technique operating individually [2, 3].

Several research studies have been implemented experimentally and numerically on heat transfer enhancement using different types of nanofluids with flow conditions categorized as turbulent. Xuan and Li [4] performed an experiment in a turbulent flow environment, all the while measuring the convective heat transfer us-

ing a uniform heat flux tube using varying concentration of Cu nanofluid which where somewhere between 0 and 2%. The results indicated a significant improvement of heat transfer coefficient, while Nusselt number also saw some enhancement when compared to the base fluid with the same Reynolds number tested. Maïga et al. [5] have implemented a numerical investigation on both saturated water and aluminum oxide (Al<sub>2</sub>O<sub>3</sub>) as the nanofluid. The investigation was identifying the hydrodynamics of the situation all the while analyzing the effect of the turbulent flow. This numerical experimentation was performed using various concentration levels using a uniform wall heat flux boundary condition. The results indicated a direct correlation between the concentration of the particles in the fluid, and the heat transfer coefficient. Namburu et al. [6] numerically analyzed three different nanofluids. These nanofluids were mixed in water and ethylene glycol in a heat flux tube of the constant form. These nanofluids were silicon dioxide, aluminum oxide, and copper (II) oxide. Based on the results, the nanoparticles that had a smaller diameter, were more viscous, and their Nusselt number was comparatively higher. This also affected the heat transfer coefficient and the pressure loss, as they both increased with the increase in concentration value. With the concentration of 6%, CuO nanofluid presents higher heat transfer performance, followed by Al<sub>2</sub>O<sub>3</sub> and SiO<sub>2</sub>. Diluted nanofluids with CuO nanoparticles of volume fractions less than 0.3% were experimentally investigated by Fotukian and Nasr Esfahany [7]. Their measurements indicated that by adding copper (II) oxide to the mix of the base fluid, there is a significant increase in heat transfer coefficient. The values were then compared with the correlation of Buongiorno [8]. Demir et al. [9] performed and experiment numerically via a simulation, on nanofluids convection flows in a constant tube wall temperature

with water/TiO<sub>2</sub> for study validation and Al<sub>2</sub>O<sub>3</sub>/water with various volume concentrations (1% and 4%) for the simulation. The results indicated that the results were agreement with a previous experiment performed by Duangthongsuk and Wongwises [10], which was the improvement of heat transfer enhancement using the water/TiO<sub>2</sub>. Sajadi and Kazemi [11] performed a similar experiment which mainly focused on the behavior of the TiO<sub>2</sub>/water. It was discovered that heat transfer rate is enhanced at certain concentration while comparing it with the base fluid of water. Kayhani et al. [12] has an experiment in a similar vein on the same nanofluid. This time, different concentration were tested, which indicated an improvement in the heat transfer coefficient as well as the volume without any great impact on the pressure drop or the Nusselt number.

In addition, there are several other studies that focus on flow pulsation on heat transfer enhancement. Numerically, Xiao et al. [13] performed an experiment which used the microtube and gas as the element within the tube. A second-order slip flow, was used as well in order to satisfy the iso flux thermal boundary condition. Based on the results from the simulation, the second-order model rarefield flow heat transfer effects were reduced. An experimental investigation performed by Koo and Kleinstreuer [14], focused on the effects of water, methanol and is-propanol on microtube and microchannel. Based on the observed results, a negative correlation occurred between the viscous dissipation and system size, as the latter decreased, the effect of the viscous dissipation on the friction factor increased. Although this study was focused on liquids, another used gaseous slip in a numerical experiment [15]. The setting revolved around the use of an infinite microtube, while the boundary conditions varied. A negative correlation was observed between the Nusselt number and Knudsen number, while a positive correlation was set for the Nusselt number and Peclet number. Another numerical investigation by Wang and Wang [16] focused on microtubes as well, however in this research the wall roughness was of main concern, particularly on a 3D scale and its effects on the laminar flow. The results showed a negative correlation between the Reynolds number and disturb areas of flow field, as the latter became larger, the first decreased in value. A research by Aziz and Niedbalski [17] simulated microtube with diluted gas flow. This simulation and numerical experiment was conducted based on the first and second order slip, and the results showed that as the fluid flowed through the cooler sections of the microtube, the value of the Nusselt number decreased.

## 2. Numerical model

### 2.1. Geometry and the governing equations

The 3-D Navier–Stokes and energy equations were used to describe the flow and heat transfer in the microtube. Fig. 1 and 2 present the computational and mesh domain for microtube model. In the Cartesian coordinates the governing equations are as follows:

$$\text{Continuity equation: } \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \quad (1)$$

Momentum:

x-direction equation :

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} = -\frac{\partial P}{\partial x} + \nu \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right) \quad (2)$$

y-direction equation:

$$u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} = -\frac{\partial P}{\partial y} + \nu \left( \frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} + \frac{\partial^2 v}{\partial z^2} \right) \quad (3)$$

z-direction equation :

$$u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} = -\frac{\partial P}{\partial z} + \nu \left( \frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial y^2} + \frac{\partial^2 w}{\partial z^2} \right) \quad (4)$$

where:

$\nu$  represent the fluid kinematic viscosity ( $\nu = \mu / \rho$ )

Energy equation:

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} + w \frac{\partial T}{\partial z} = \alpha \left( \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right) \quad (5)$$

where:

$\alpha$  represent the fluid thermal diffusivity ( $\alpha = k/\rho C_p$ ).

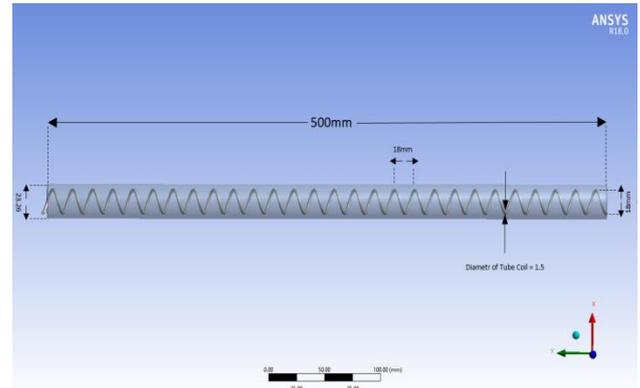


Fig. 1: Micro tube model

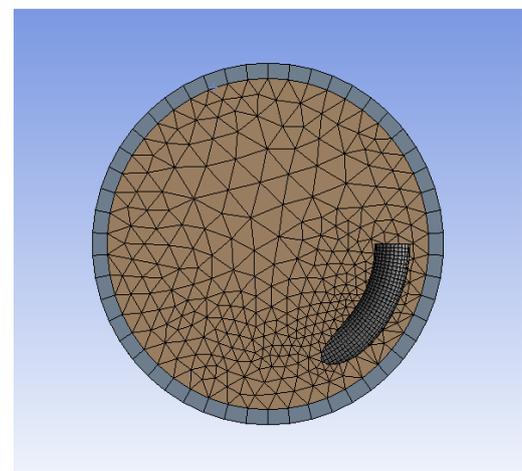


Fig. 2: Meshed Micro tube model

### 2.2. Thermophysical properties of nanofluids

In order to obtain the properties the used nanofluids in terms of their thermophysical nature, equation 6 through 10 were used.

For the density

The density of nanofluid  $\rho_{nf}$  can be obtained from the following equation [18]

$$\rho_{nf} = (1 - \phi)\rho_f + \phi\rho_{np} \quad (6)$$

where :

$\rho_f$  and  $\rho_{np}$  are the mass densities of the based fluid and the solid nanoparticles, respectively.

For the heat capacity

The effective heat capacity at constant pressure of nanofluid, can be calculated from the following equation [19]

$$(\rho c_p)_{nf} = (1 - \phi)(\rho c_p)_f + \phi(\rho c_p)_{np} \quad (7)$$

where:

$(\rho c_p)_f$  and  $(\rho c_p)_{np}$  are the heat capacities of the based fluid and the solid nanoparticles, respectively

For Effective thermal conductivity

By using Brownian motion of nanoparticles, the effective thermal conductivity can be obtained by using the following mean empirical correlation [18]

$$K_{static} = K_{static} + K_{Brownian} \tag{8}$$

$$K_{static} = K_f \left| \frac{v_{np} + v_{f}}{v_{f}} - \frac{v_{np}}{v_{f}} \right| \tag{9}$$

$$k_{Brownian} = 5 \times 10^4 \beta \phi \rho_f C_{p,ns} \left| \frac{kT}{v_{f}} \right| f(T, \phi) \tag{10}$$

where:

Boltzmann constant:  $k = 1.3807 \times 10^{-23} \frac{J}{K}$

Modelling,  $f(T, \phi)$

$$f(T, \phi) = (2.8217 \times 10^{-2} \phi + 3.917 \times 10^{-2}) \left( \frac{T}{T_0} \right) + (-3.669 \times 10^{-2} \phi - 3$$

For Effective viscosity

The effective viscosity can be obtained by using the following mean empirical correlation [19]

$$\mu_{eff} = \mu_f \times \frac{1}{1 - 3} \tag{11}$$

$$d_f = \left| \frac{6M}{N} \right|^{1/3} \tag{12}$$

where M is the molecular weight of base fluid, N is the Avogadro number =  $6.022 \times 10^{23} \text{ mol}^{-1}$ ,  $\rho_f$  is the mass density of the based fluid calculated at temperature  $T_0=293K$ .

### 2.3. Numerical method and grid testing

In order to address the issue of continuity, an approach known as finite volume was used. However, this also addresses the momentum and aforementioned energy equations, as well as the boundary conditions. As the study required a grid size for the geometry, a test known as the grid independence is used to obtain those metrics. Four different sizes were used for the grid, these were 3915382, 4287098, 4423552 and 5000000, all of which demonstrated to have only slightly affected on the Nusselt number. For this reason, the size that was ultimately used was the 4423552 as it apparently provided a better grid independent solution according to the simulation.

## 3. Result and discussion

### 3.1. Effect of Micro coil pitch

The influence of micro coil pitch (10mm, 14mm, and 18mm) on Nusselt number, skin friction factor and thermal performance using water as test fluid are shown in Figs. 3, 4 and 5. Apparently from Fig. 3, micro coil with pitch 10mm exhibits higher Nusselt number than others. The reason behind this is that micro coil with pitch 10mm generates swirl flow with efficient fluid mixing near-by their alternative curvature and with tube wall. From Fig. 4, it can be seen that friction factor decreases with Reynolds number and increase with decreasing of coil pitch. This implies that the influence of nearest alternative pitch along the pipe promotes additional wall shear stress due to flow mixing between the fluid and tube wall. Fig. 5 shows the variation of thermal performance factor with Reynolds number. The values of thermal performance factor increase with Reynolds number and pitch. This is an indication of the energy saving feasibility of the micro coil when using the turbulent flow. It is also evident that the thermal performance factor for 18mm pitch value at constant Reynolds number is higher than others. This because the turbulence/swirl flow generated a long the coil as it became stronger.

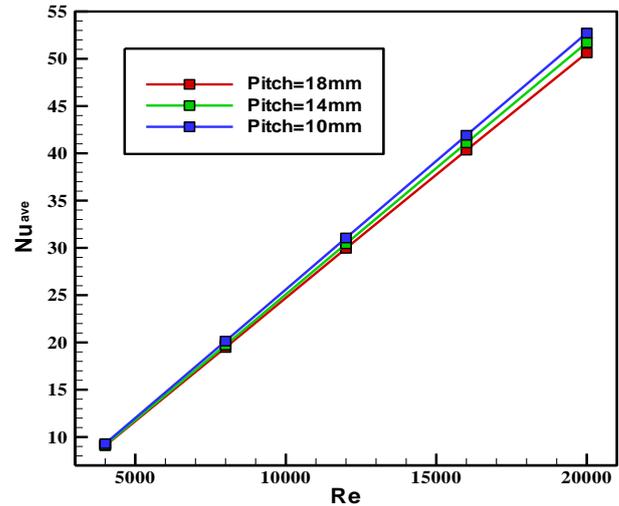


Fig. 3: Variation of the Nusselt number vs Reynolds number with different coil pitch and diameter

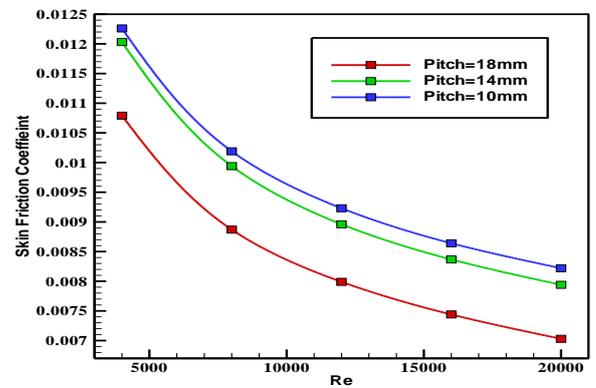


Fig. 4: Variation of the skin friction factor vs Reynolds number with different coil pitch and diameter

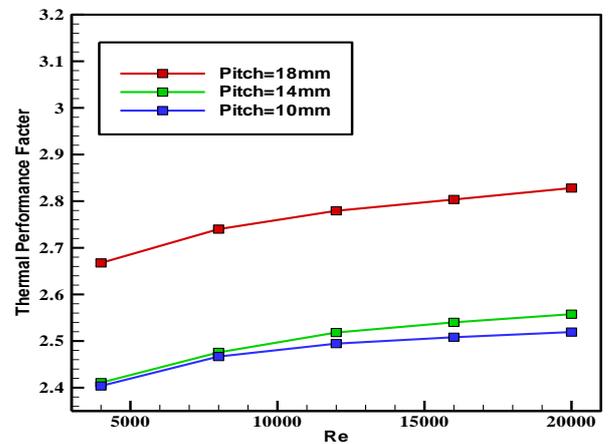


Fig. 5: Variation of the thermal performance factor vs Reynolds number with different coil pitch and diameter

### 3.2. Effect of nanoparticle concentrations

Variations of heat transfer coefficient and friction factor versus Reynolds number for water,  $Al_2O_3$  and  $CuO$  nanofluids of 1% and 2% volume concentration by fixing the coil pitch value (18mm) are shown in Figs. 6 and 7. Evidently, Fig. 6 shows that the combined use of nanofluid with micro coil produces further augment in heat transfer coefficient than water. The simultaneous use of nanofluid with coil increases the thermal conductivity and viscosity of working fluid as well as increasing swirl flow path. Thus, greater fluid mixing and higher heat transfer coefficient are produced. Eventually,  $Al_2O_3$  nanofluid with 2% volume concentration offered a higher heat transfer coefficient compared with the

others. Figure 7 demonstrates a negative correlation between the Reynolds number and the friction factor, regardless of the fluid used, since both the water and different nanoparticles seem to exhibit the same effect. As Reynolds number is increased, the friction coefficient is reduced. This phenomenon is attributed to the increase in viscosity and concentration, which in turn increase the wall shear stress. As it can be seen, the low viscosity has contributed in making water lower than other nanofluids when it comes shear stress value. An increase in pressure drop has also been noted to correlate positively with viscosity. However, the simulated results seem to indicate no correlation between nanofluid concentration and pressure drop, as the friction factor exhibits no significant change.

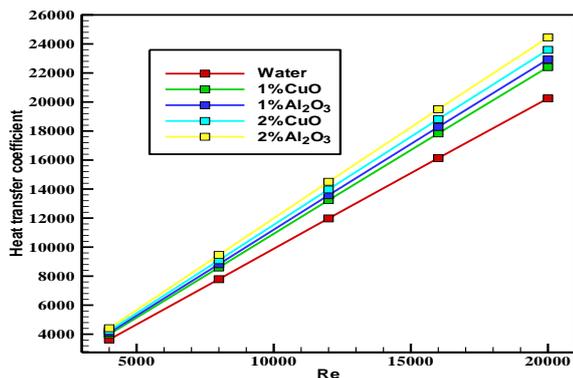


Fig. 6: Variation of the heat transfer coefficient vs Reynolds number

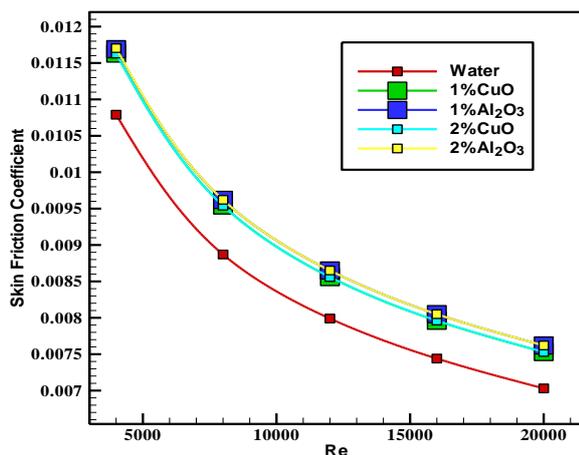


Fig. 7: Variation of the skin friction factor vs Reynolds number

## 4. Conclusion

In this study, a simulated and numerical study was conducted on a micro coil using a variety of different fluids and nanofluids. The main fluid used was water, with nanofluids such as aluminum oxide and copper (II) oxide. The study focused on measuring the effect of different concentrations for the nanofluids, while different Reynold numbers were incorporated. The results indicated that:  $\text{Al}_2\text{O}_3$  (aluminum oxide) exhibited to have the highest heat transfer coefficient. It also noted that the velocity and pressure drop were the highest value among the tested fluids, although the friction factor seemed to remain unchanged.

The highest heat transfer coefficient, velocity, wall shear stress and pressure drop increase as the percentage of concentration ( $\phi$ ) increases. Based on the recorded results, there is no direct correlation between the concentration of the particles and friction factor. The Reynolds number is also recorded to have an effect on the Nusselt number, with a positive correlation. As one increases, so does the other. This also applies to Reynolds number and other

properties such as heat transfer coefficient, velocity, and wall shear stress, as well as pressure drop.

The Reynolds number was recorded to have a negative correlation with the friction factor, as the highest Reynolds number led to the recording of the lowest friction factor.

The final conclusion is that the aluminum oxide seems to have the highest effect on the parameters and led to more positive and desirable results. This occurred at a 2% concentration, alongside a 25nm for the dp, using 20000 as the Reynolds number.

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## Nomenclature

$\text{Al}_2\text{O}_3$	Aluminum oxide
$C_p$	Specific heat of the fluid, J/kg K
CuO	Copper oxide
$d_f$	Diameter of base fluid molecule
$d_p$	Nanoparticle diameter, m
$g$	Gravitational acceleration, m/s <sup>2</sup>
$k$	Thermal conductivity, W/m K
$k_{eff}$	Effective thermal conductivity
$M$	Molecular weight of base fluid
$N$	Avogadro number, $N=6.022 \times 10^{23} \text{mol}^{-1}$
$Nu$	Nusselt number, $Nu=hD/k$
$P$	Pressure of fluid, Pa
$Pr$	Prandtl number, $Pr=C_p \mu/k$
$Re$	Reynolds number, $Re=\rho u D/\mu$
$T$	Temperature of fluid, K
$T$	Bulk temperature, K
$T_0$	Reference temperature

### Greek symbols

$\mu_{eff}$	Effective viscosity
$\alpha$	Thermal diffusivity, m <sup>2</sup> /s
$\mu$	Dynamic viscosity of fluid, kg/m s
$\nu$	Kinematic viscosity of fluid, m <sup>2</sup> /s
$\rho$	Fluid density, kg/m <sup>3</sup>
$\phi$	Volume fraction of nanoparticles

### Subscript

bf	Base-fluid
nf	Nanofluids
np	Nanoparticle
eff	Effective

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